

# Sumatra Earthquake and Earth Rotation

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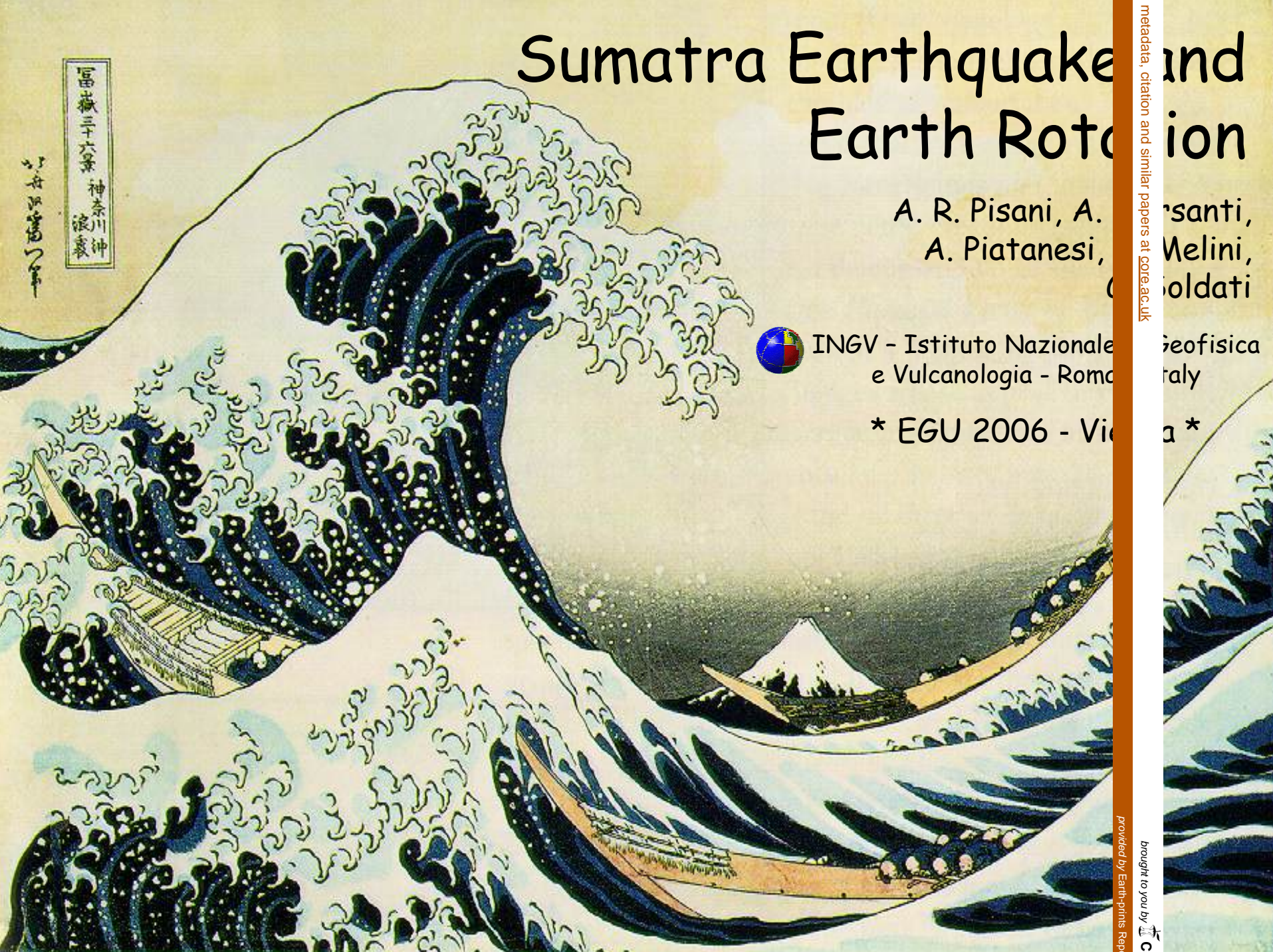


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\* EGU 2006 - Vienna \*

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On 26th December 2004 off the west coast of northern Sumatra occurred one of the most devastating earthquakes of the modern history.

In correspondence of the event, a step discontinuity in the instantaneous rotational pole path has been evidenced by means of SLR and GPS techniques.

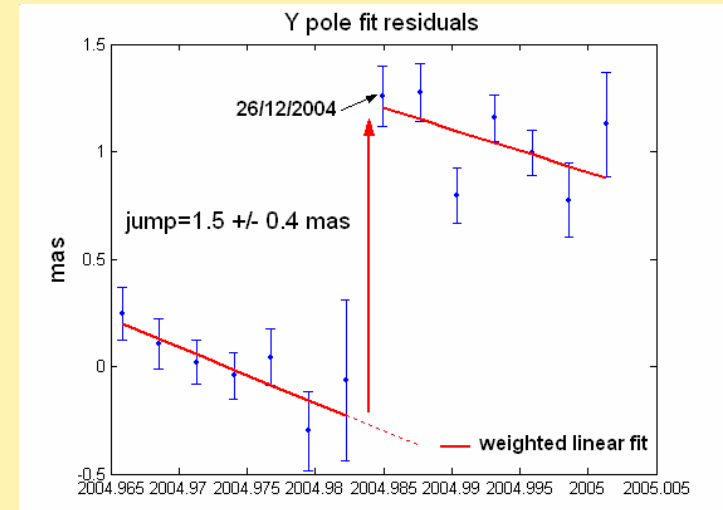
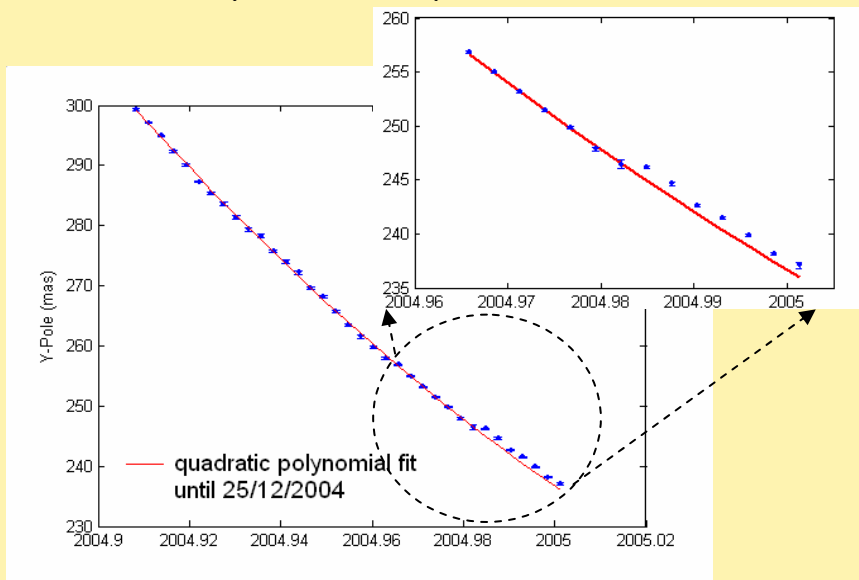
- Sumatra is probably the largest event since the giant Chile earthquake (1960).
- There has been a great improvement of the accuracy in the pole position detecting techniques since 1960.

Sumatra earthquake seems to be the best candidate to study the effects given by a seismic event on polar motion.



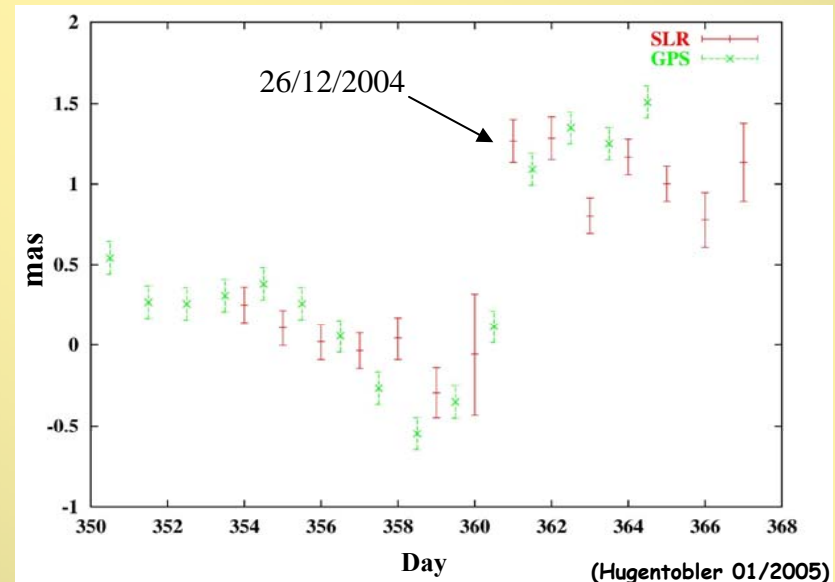
## *Geodetic evidences of the step discontinuity in the pole path.*

On 19th January 2005 the International Laser Ranging Service (ILRS) provided preliminary estimates about the earthquake effect on pole motion.



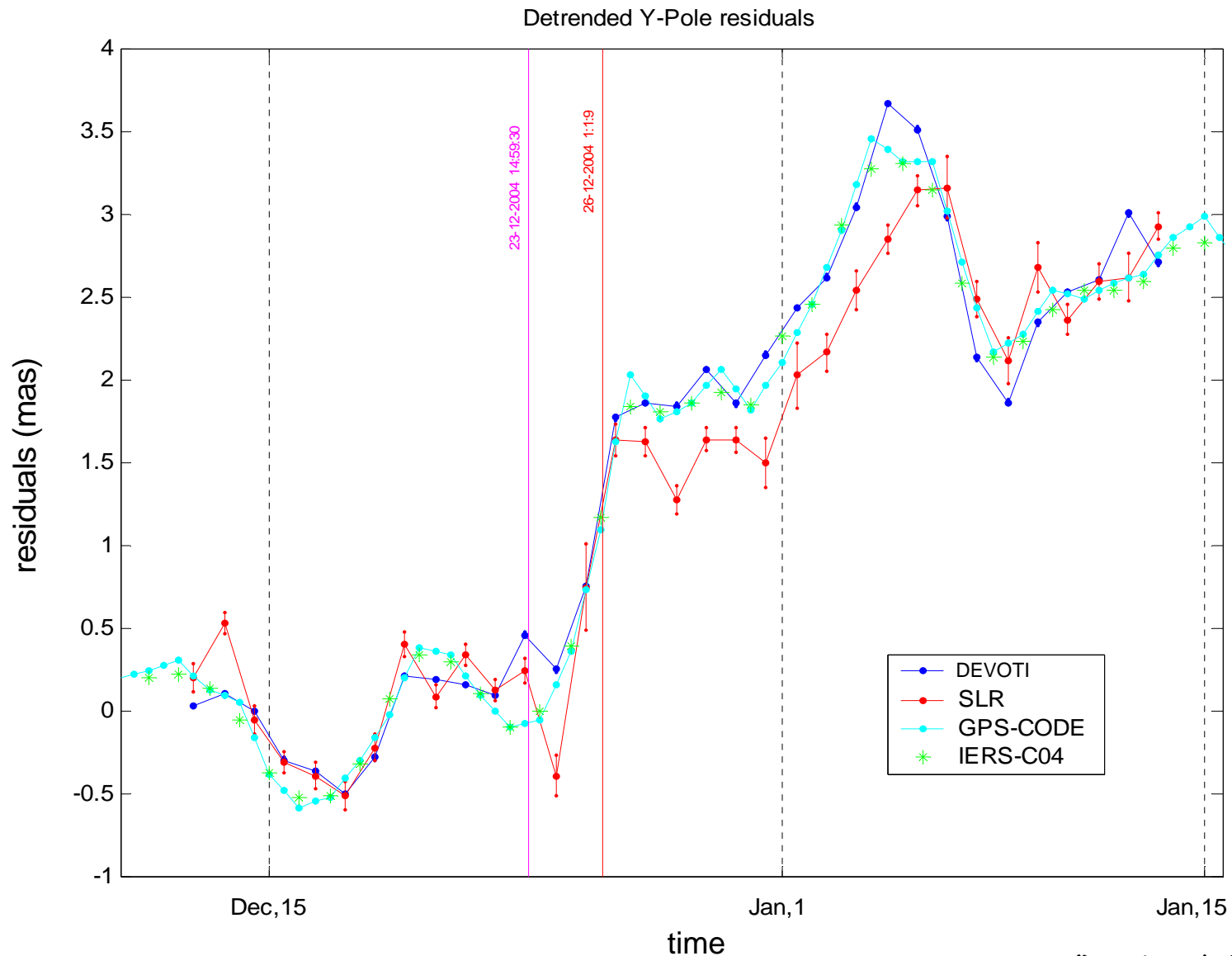
(Bianco, Luceri, Sciarretta 12/2004)

These estimations, based on SLR technique and then compared with GPS data, revealed a step discontinuity of about 1.5-2.0 mas in the y-component of the instantaneous rotational pole in correspondence of Sumatra earthquake.



(Hugentobler 01/2005)

A more recent study (09/2005) shows that independent solutions, retrieved by means different techniques, give a coherent measure of the y-pole displacement during the Sumatra event.



(Devoti et al. 09/2005)



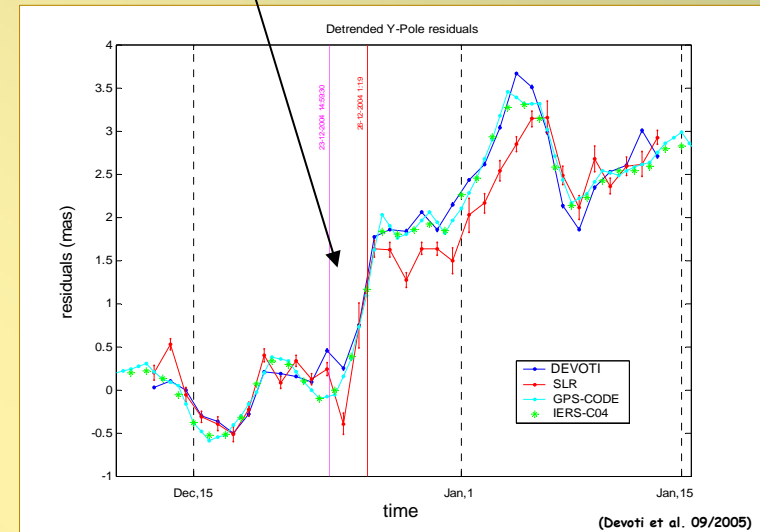
$$\Psi(t) = \Delta \Psi H(t)$$

The diagram shows a mechanism in a coordinate system with axes  $x_1$  (vertical, pointing down) and  $x_2$  (horizontal, pointing right). A slider block, consisting of points  $A$ ,  $B$ , and  $C$ , moves along the  $x_1$  axis. Point  $A$  is at the origin,  $B$  is on the  $x_1$  axis, and  $C$  is above  $B$ . A curved path, representing a cam profile, is shown in the lower-right quadrant. Two points on this path are labeled  $P_1$  and  $P_2$ . A line segment connects  $C$  to  $P_2$ . A curved arrow labeled  $\omega$  indicates the angular velocity of the arm  $CP_2$ .

Lambeck, 1980

# What did cause the step-like discontinuity in the pole path?

❖ The jump in the instantaneous rotation pole path is compatible with an excitation function characterized by a delta-like temporal dependence which is produced by a transient *mass redistribution*.



We want to test the hypothesis that the perturbation to the inertia tensor, which produced such discontinuity in the pole path, has been caused by the

*transient water mass redistribution produced by the TSUNAMI.*


To evaluate the discontinuity in the pole path produced by the tsunami we have to solve the instantaneous rotational pole motion equation:

$$\mathbf{m}(t) = m_x(t) + jm_y(t) = -j\sigma_0 \frac{k_0}{k_2 - k_0} e^{j\sigma_0 t} \int_t \Psi_{tsunami}(\tau) e^{-j\sigma_0 \tau} d\tau$$

$\sigma_0$  = Chandler frequency;

$\frac{k_0}{k_0 - k_2}$  = correction given by the elastic deformation of the rotational Earth;

$\Psi_{tsunami}$  is the *excitation function* that includes the *perturbation associated to the mass redistribution* given by the TSUNAMI and its form is:

$$\Psi_{tsunami} = \Psi_m + \Psi_v$$


The diagram shows two arrows originating from the equation  $\Psi_{tsunami} = \Psi_m + \Psi_v$ . One arrow points down and to the left towards the 'Mass term' box, and the other points down and to the right towards the 'Velocity term' box.

### Mass term

associated to the static redistribution of mass caused by the variation of sea surface.

### Velocity term

associated to the exchange of angular momentum between the Earth and the horizontal flowing water.

To evaluate the instantaneous rotational pole motion  $\mathbf{m}(t)$  first of all we need to calculate the excitation function associated with the tsunami:

$$\Psi_{tsunami} = \Psi_m + \Psi_v$$

*Mass Term:  
vertical water  
displacement.*

*Velocity Term:  
horizontal velocity  
field.*

$$\begin{cases} \Psi_{mx} = - \int_{V_w} \frac{\rho_w}{C-A} r^2 \cos \phi \sin \phi \cos \lambda dV \\ \Psi_{my} = - \int_{V_w} \frac{\rho_w}{C-A} r^2 \cos \phi \sin \phi \sin \lambda dV \end{cases}$$

$$\begin{cases} \Psi_{vx} = - \int_{V_w} \frac{2\rho_w}{\Omega(C-A)} r \sin \phi (u_\lambda \cos \lambda - u_\phi \sin \phi \sin \lambda) dV \\ \Psi_{vy} = + \int_{V_w} \frac{2\rho_w}{\Omega(C-A)} r \sin \phi (-u_\lambda \sin \lambda - u_\phi \sin \phi \cos \lambda) dV \end{cases}$$

$\phi, \lambda$  Latitude and longitude.

$u_\phi, u_\lambda$  Horizontal Velocity Components.

$A, C, \Omega$  Equatorial and polar inertia momentum, angular velocity of the Earth.

$\rho_w$  Oceanic water density.

$\Psi_m, \Psi_v$  have been evaluated using a  
*synthetic numerical tsunami model* which gives:

\*Vertical displacement of the water

\*Horizontal velocity field

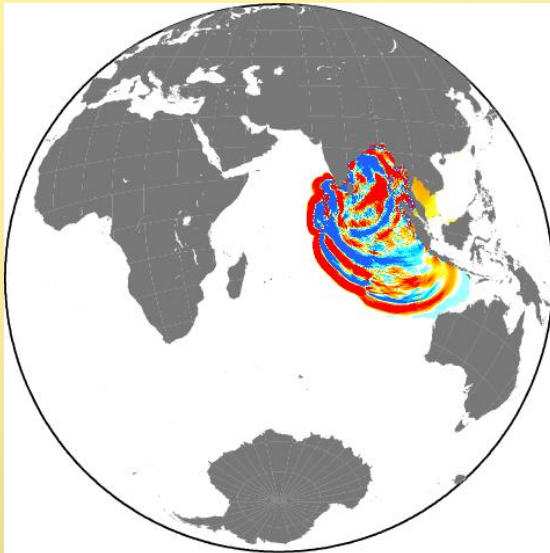
in the propagation area of the tsunami, in a time window of 16 hours.

(An area of about  $10^8 \text{ Km}^2$  ( $-75^\circ < \phi < 30^\circ$  and  $0^\circ < \lambda < 150^\circ$ ) sampled into a grid of  $2'$ )

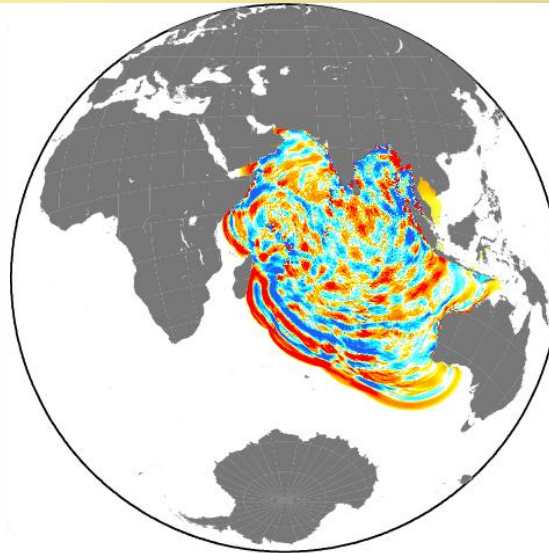


# *Snapshots of the tsunami propagation from the numerical model at different time steps.*

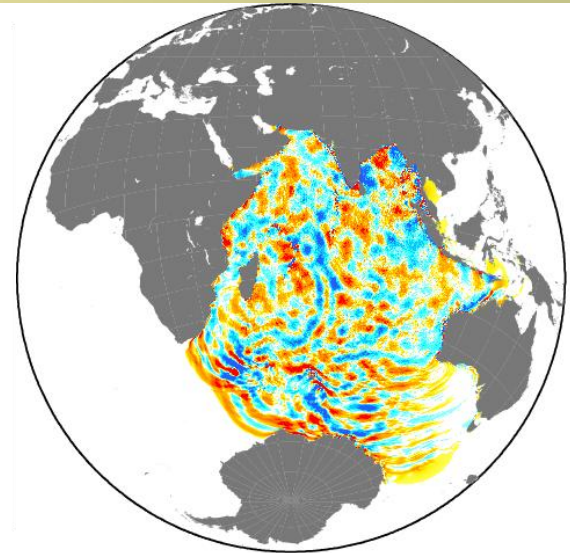
Elevation



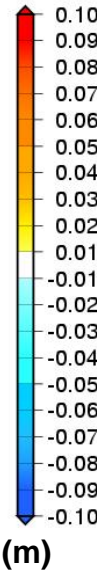
time = 4. hours



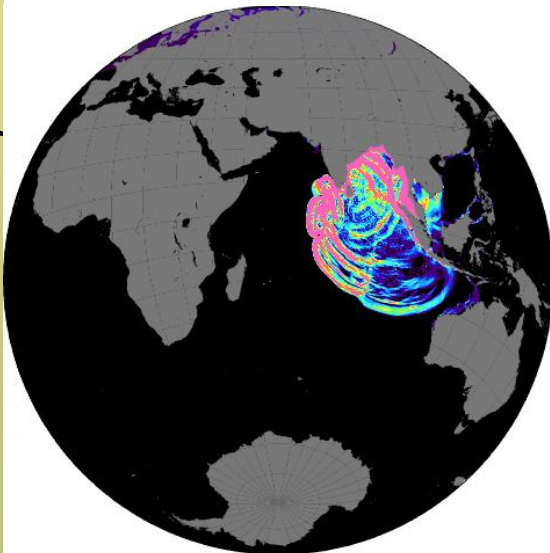
time = 8. hours



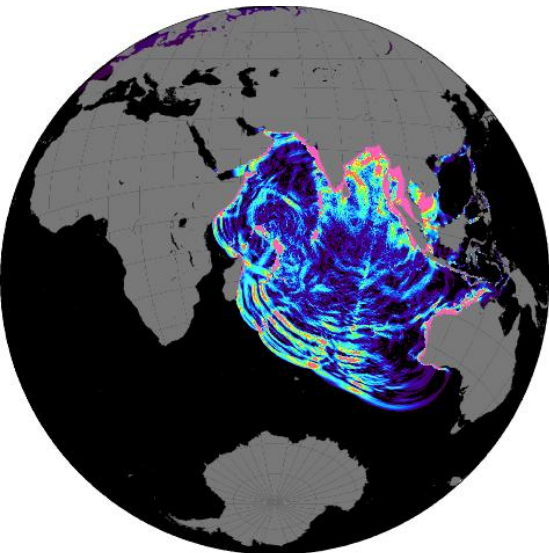
time = 12. hours



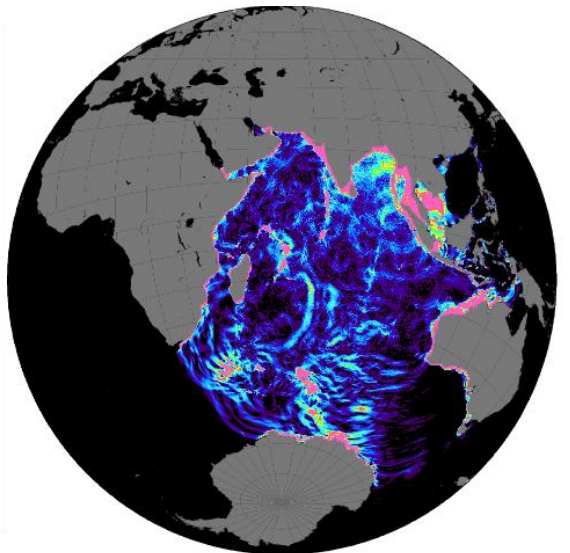
Horizontal Velocity Field



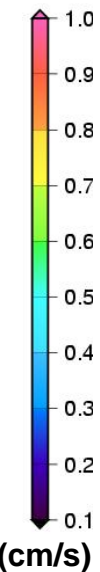
time = 4. hours



time = 8. hours



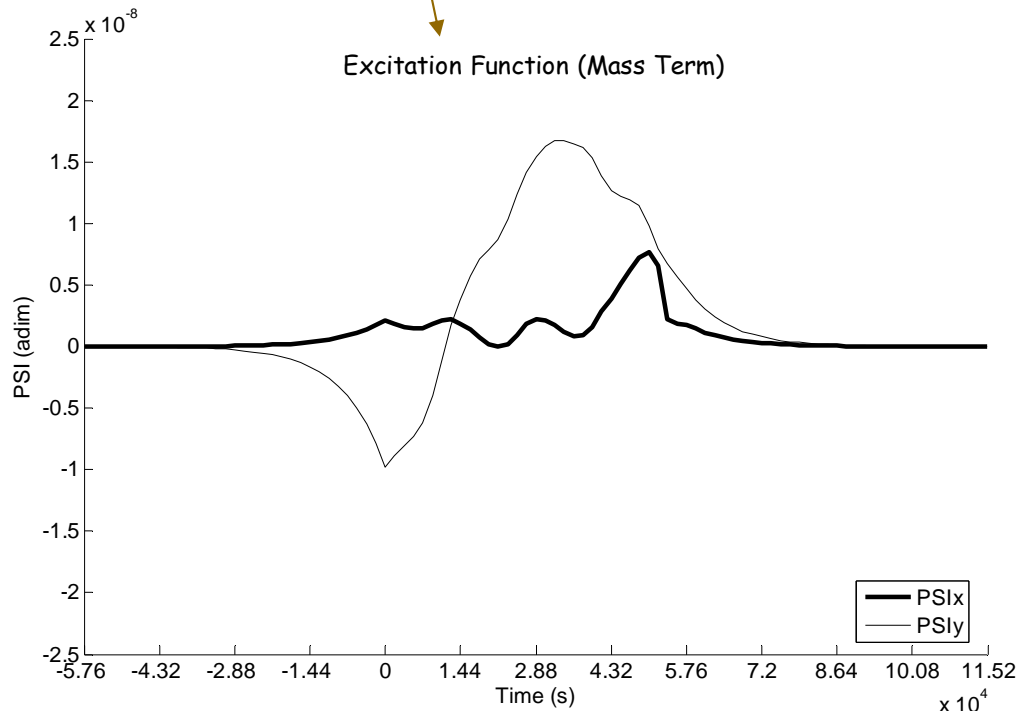
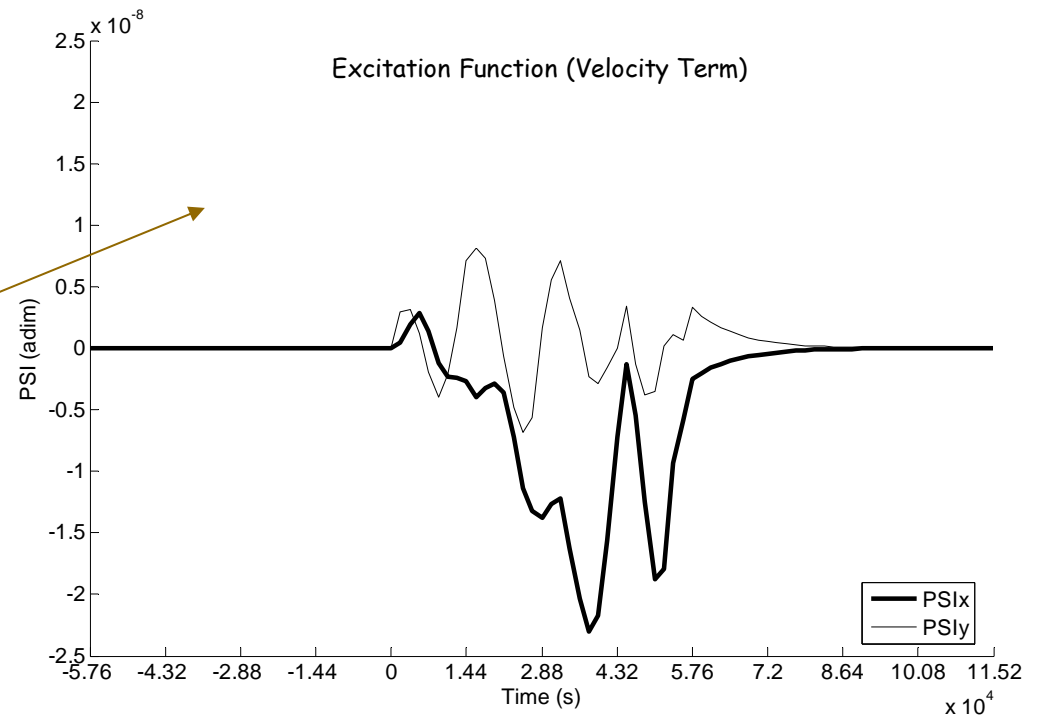
time = 12. hours



(Piatanesi, 2006)

From the synthetic  
numerical tsunami  
model:

$$\Psi_{tsunami} = \Psi_m + \Psi_v$$

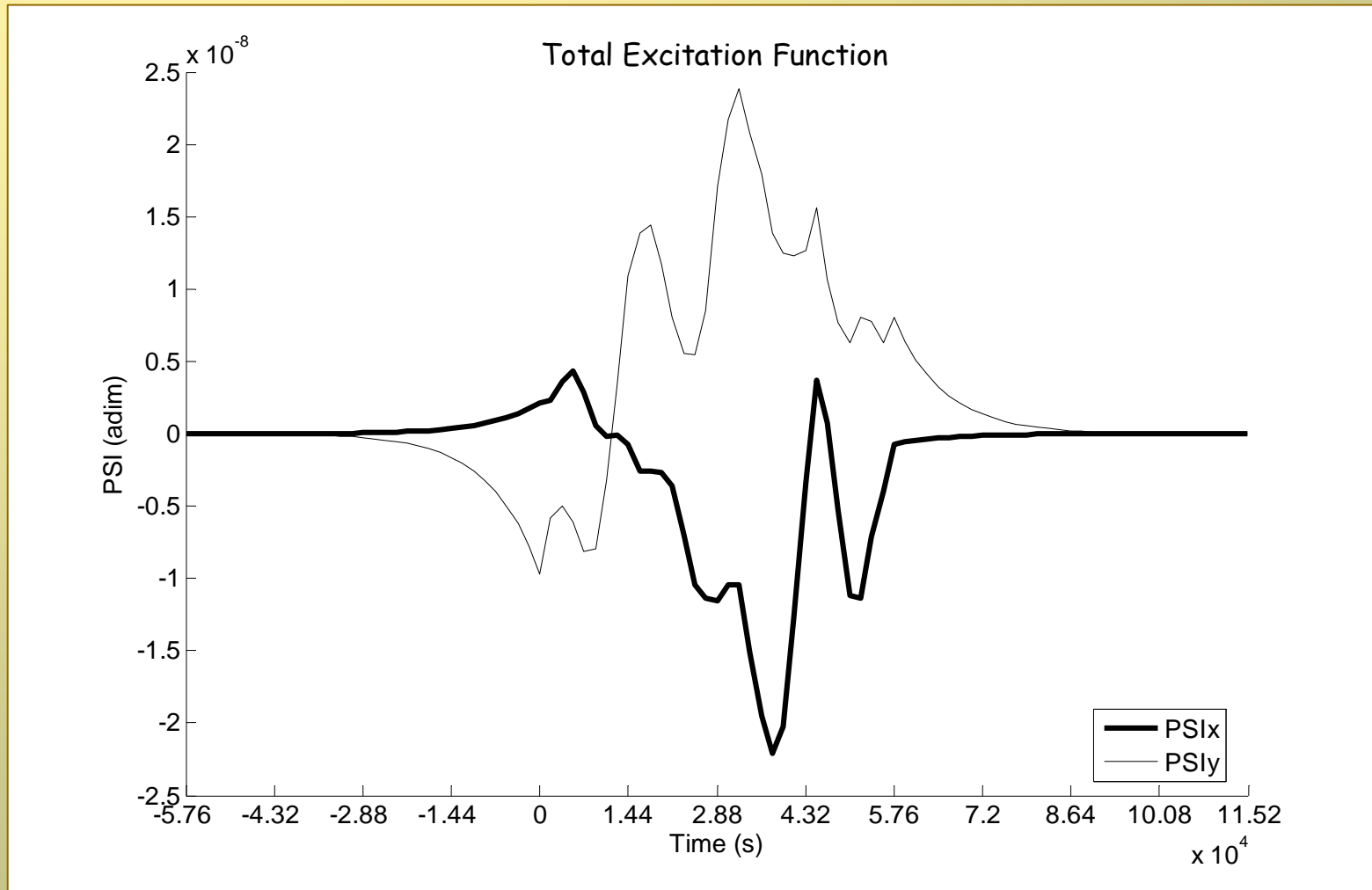


Trends of the two  
different  
contributions given  
to the total  
excitation function  
by the *mass term*  
and the *velocity*  
*term*.

## Total excitation function.

$$\Psi_{tsunami} = \Psi_m + \Psi_v$$

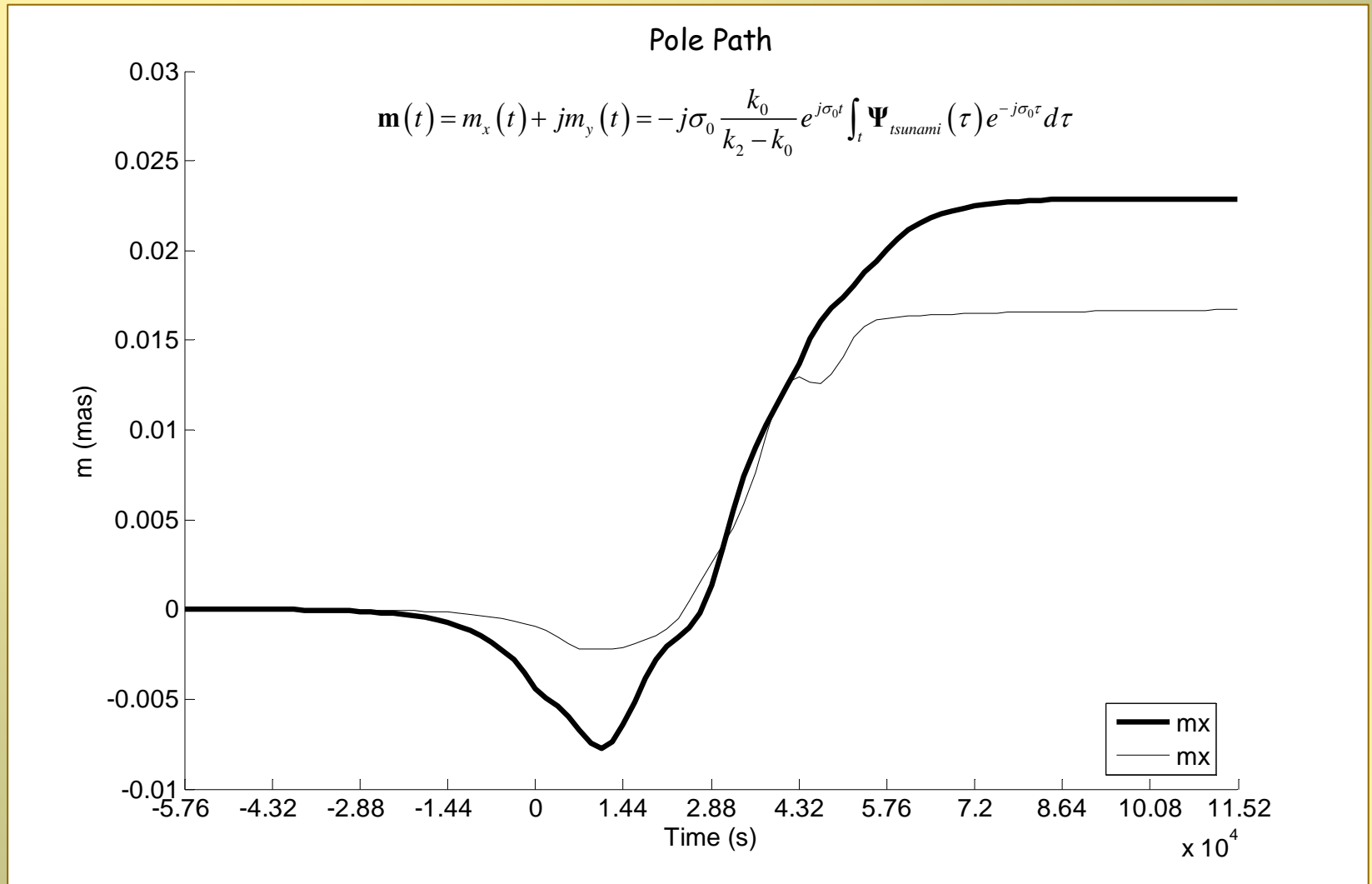
(Excitation pole or mean pole of rotation around which revolves the instantaneous rotational pole)



A delta-like temporal dependence that we were looking for  
to obtain the observed pole path displacement.

Solving the instantaneous rotational pole motion equation we obtained

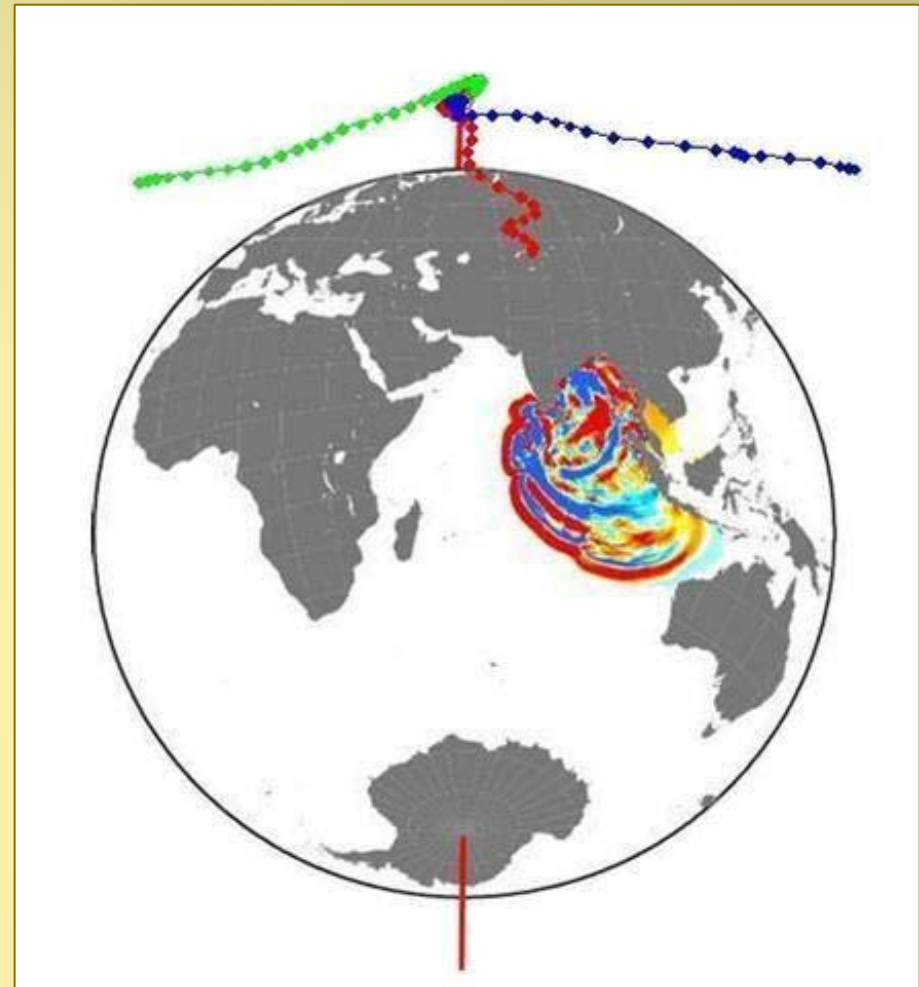
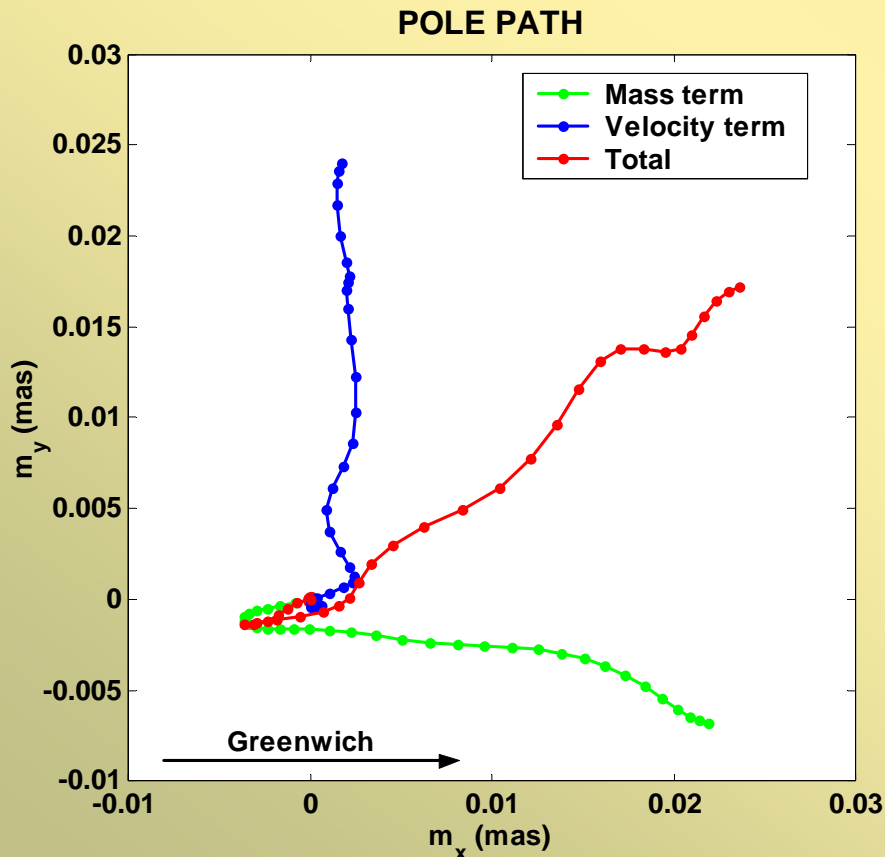
Pole path variations associated with the excitation function  $\Psi_{tsunami}$



❖ Shift in the pole path from  $\left\{ \begin{array}{l} \text{our simulations: } \sim 3.3 \cdot 10^{-2} \text{ mas} \\ \text{geodetic techniques: } \sim (1.5 - 2.0) \text{ mas} \end{array} \right.$



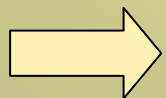
Pole path after  
the occurrence  
of the Tsunami.



Pole paths overlapped to the  
planisphere.

# Summary

- ❖ Geodetic data evidenced a discontinuity in the y-component of the instantaneous rotational pole path in correspondence of Sumatra earthquake.
- ❖ We assumed that such discontinuity has been caused by a perturbation to the inertia tensor associated with the mass redistribution due to the tsunami.
- ❖ The total excitation function and the perturbation to the pole path, have been obtained using a synthetic numerical tsunami model that gave us:
  - excitation function values due to the vertical displacement of the water;
  - excitation function values due to the horizontal velocity field of the flowing water.
- ❖ Finally, our simulations show:
  - ✓ the simulated shift in the pole path is 50 times smaller than that observed in geodetic data;



*Shift in the pole path is not due to the mass redistribution caused by the tsunami.*

❖ Nevertheless, the results of our analysis cannot be considered conclusive for three main reasons:

1. Dragging effects could play an important role in exchanging angular momentum between Ocean and solid Earth during the propagation of the tsunami wave.  
Presently we are not able to include this effects in our numerical simulations.
2. We observed an increase of perturbation in correspondence of an increase of resolution of the grid used to sample the propagation area. (This is probably due to dispersion artefacts in the computed wavefield strongly dependent from the domain resolution). Two arc minutes is now the maximum resolution affordable by our numerical routines, but it is possible that further increase in the resolution would result in an increase in the computed perturbation too.
3. The elevation of a tsunami wave has been subject to several investigations and also experimental observations, for this reason while we can consider the output of the simulations, concern with water elevations, highly reliable, this is not true for the output of the simulations concern with the velocity field of the horizontal flow.



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浪裏

ふじさん

Thanks for your attention

